Stoichiometry

So far in your chemistry course, you have learned that chemists count quantities of elements and compounds in terms of moles and that they relate moles of a substance to mass by using the molar mass. In addition, you have learned to write chemical equations so that they represent the rearrangements of atoms that take place during chemical reactions, and you have learned to balance these equations. In this chapter you will be able to put these separate skills together to accomplish one of the most important tasks of chemistry - using chemical equations to make predictions about the quantities of substances that react or are given off as products and relating those quantities to one another. This process of relating quantities of reactants and products in a chemical reaction to one another is called stoichiometry.

First, look at an analogy.

Suppose you need to make several sandwiches to take on a picnic with friends. You decide to make turkey-and-cheese sandwiches using the following "equation:"

2 bread slices + 2 turkey slices + 1 lettuce leaf

+ 1 cheese slice \rightarrow 1 turkey-and-cheese sandwich

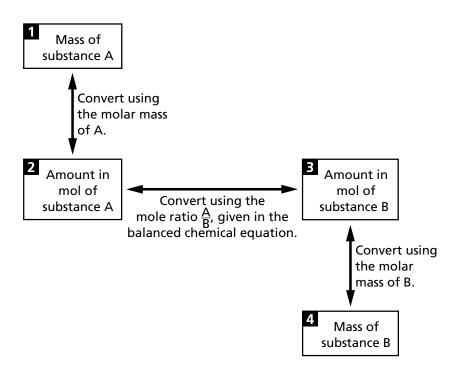
This equation shows that you need those ingredients in a ratio of 2:2:1:1, respectively. You can use this equation to predict that you would need 30 turkey slices to make 15 sandwiches or 6 cheese slices to go with 12 turkey slices.

Zinc reacts with oxygen according to the following balanced chemical equation:

$$2Zn + O_2 \rightarrow 2ZnO$$

Like the sandwich recipe, this equation can be viewed as a "recipe" for zinc oxide. It tells you that reacting two zinc atoms with a molecule of oxygen will produce two formula units of zinc oxide. Can you predict how many zinc oxide units could be formed from 500 zinc atoms? Could you determine how many moles of oxygen molecules it would take to react with 4 mol of zinc atoms? What if you had 22 g of zinc and wanted to know how many grams of ZnO could be made from it? Keep in mind that the chemical equation relates amounts, not masses, of products and reactants. The problems in this chapter will show you how to solve problems of this kind.

General Plan for Solving Stoichiometry Problems



SAMPLE PROBLEM 1

Ammonia is made industrially by reacting nitrogen and hydrogen under pressure, at high temperature, and in the presence of a catalyst. The equation is $N_2(g) + 3H_2(g) \rightarrow 2NH_3(g)$. If 4.0 mol of H₂ react, how many moles of NH₃ will be produced?

SOLUTION

1. ANALYZE

• What is given in the problem?

the balanced equation, and the amount of H₂ in moles

• What are you asked to find?

the amount of NH₃ produced in moles

Organization of data is extremely important in dealing with stoichiometry problems. You will find that it is most helpful to make data tables such as the following one.

Items	Data	
Substance	H ₂	NH ₃
Coefficient in balanced equation	3	2
Molar mass	NA*	NA
Amount	4.0 mol	? mol
Mass of substance	NA	NA

^{*} NA means not applicable to the problem

2. PLAN

- What steps are needed to that can be produced from $4.0 \text{ mol } H_2$?
- Multiply by the mole ratio of NH₃ calculate the amount of NH₃ to H₂ determined from the coefficients of the balanced equation.

Amount of
$$H_2$$
 in mol multiply by mole ratio: $\frac{NH_3}{H_2}$ Amount of $\frac{NH_3}{H_2}$ NH₃ in mole

$$\begin{array}{l} \text{mol H}_{2} \times \frac{2 \hspace{0.1cm} \text{mol NH}_{3}}{3 \hspace{0.1cm} \text{mol H}_{2}} = \text{mol NH}_{3} \end{array}$$

3. COMPUTE

$$4.0 \text{ mol H}_2 \times \frac{2 \text{ mol NH}_3}{3 \text{ mol H}_2} = 2.7 \text{ mol NH}_3$$

- **4.** EVALUATE
 - Are the units correct?

Yes; the answer has the correct units of moles NH₃.

• Is the number of significant figures correct?

Yes; two significant figures is correct because data were given to two significant figures.

• *Is the answer reasonable?*

Yes; the answer is 2/3 of 4.0.

PRACTICE

1. How many moles of sodium will react with water to produce 4.0 mol of hydrogen in the following reaction?

 $2\text{Na}(s) + 2\text{H}_2\text{O}(l) \rightarrow 2\text{NaOH}(aq) + \text{H}_2(g)$ ans: 8.0 mol Na

2. How many moles of lithium chloride will be formed by the reaction of chlorine with 0.046 mol of lithium bromide in the following reaction?

 $2\text{LiBr}(aq) + \text{Cl}_2(g) \rightarrow 2\text{LiCl}(aq) + \text{Br}_2(l)$ ans: 0.046 mol LiCl

3. Aluminum will react with sulfuric acid in the following reaction.

 $2\text{Al}(s) + 3\text{H}_2\text{SO}_4(l) \rightarrow \text{Al}_2(\text{SO}_4)_3(aq) + 3\text{H}_2(g)$

- a. How many moles of H₂SO₄ will react ans: 27 mol H₂SO₄ with 18 mol Al?
- **b.** How many moles of each product ans: 27 mol H₂ will be produced? 9 mol $Al_2(SO_4)_3$
- **4.** Propane burns in excess oxygen according to the following reaction.

$$C_3H_8 + 5O_2 \rightarrow 3CO_2 + 4H_2O$$

- a. How many moles each of CO₂ and H₂O ans: 11.6 mol CO₂ are formed from 3.85 mol of propane? 15.4 mol H₂O
- ans: 0.388 mol CO₂ **b.** If 0.647 mol of oxygen are used in the burning of propane, how many moles 0.518 mol H₂O each of CO₂ and H₂O are produced? How 0.129 mol C₃H₈ many moles of C₃H₈ are consumed?

SAMPLE PROBLEM 2

Potassium chlorate is sometimes decomposed in the laboratory to generate oxygen. The reaction is $2KClO_3(s) \rightarrow 2KCl(s) + 3O_2(g)$. What mass of KClO₃ do you need to produce 0.50 mol O₂?

SOLUTION

- 1. ANALYZE
 - What is given in the the amount of oxygen in moles problem?
 - What are you asked to find? the mass of potassium chlorate

Items	Data	
Substance	KCIO ₃	O ₂
Coefficient in balanced equation	2	3
Molar mass*	122.55 g/mol	NA
Amount	? mol	0.50 mol
Mass	? g	NA

^{*} determined from the periodic table

2. PLAN

- What steps are needed to calculate the mass of KClO₃ needed to produce $O.50 \text{ mol } O_2$?
- Use the mole ratio to convert amount of O2 to amount of KClO₃. Then convert amount of KClO₃ to mass of KClO₃.

2 Amount of O₂ in mol multiply by mole ratio ➤ Amount of KClO₃ in mol 2 mol KClO3 multiply by molar mass $3 \bmod O_2$ of KClO

Mass of KClO₃ in g

$$\begin{array}{l} \underset{mol\ O_{2}}{\text{mol}\ ClO_{3}} \times \frac{2\underset{mol\ KClO_{3}}{\text{mol}\ KClO_{3}}}{3\ mol\ O_{2}} \times \frac{122.55\underset{g\ KClO_{3}}{\text{mol}\ KClO_{3}}}{1\ mol\ KClO_{3}} = g\ KClO_{3} \end{array}$$

3. COMPUTE

$$0.50 \text{ mol } O_2 \times \frac{2 \text{ mol KClO}_3}{3 \text{ mol } O_2} \times \frac{122.55 \text{ g KClO}_3}{1 \text{ mol KClO}_3} = 41 \text{ g KClO}_3$$

4. EVALUATE

- Are the units correct? Yes; units canceled to give grams of KClO₃.
- Yes; two significant figures is • Is the number of significant figures correct? correct.
- Yes; 41 g is about 1/3 of the molar • *Is the answer reasonable?* mass of KClO₃, and $0.5 \times 2/3 =$ 1/3.

PRACTICE

1. Phosphorus burns in air to produce a phosphorus oxide in the following reaction:

$$4P(s) + 5O_2(g) \rightarrow P_4O_{10}(s)$$

- a. What mass of phosphorus will be needed to produce 3.25 mol of P_4O_{10} ? ans: 403 g P
- **b.** If 0.489 mol of phosphorus burns, what ans: 19.6 g O₂ mass of oxygen is used? What mass of 15.4 g P₂O₄ P₄O₁₀ is produced?
- 2. Hydrogen peroxide breaks down, releasing oxygen, in the following reaction:

$$2H_2O_2(aq) \rightarrow 2H_2O(l) + O_2(g)$$

a. What mass of oxygen is produced when 1.840 mol of H₂O₂ decompose? ans: 29.44 g O_2

b. What mass of water is produced when $5.0 \text{ mol } O_2 \text{ is produced by this reaction?}$ ans: 180 g H₂O

SAMPLE PROBLEM 3

How many moles of aluminum will be produced from 30.0 kg Al₂O₃ in the following reaction?

$$2Al_2O_3 \rightarrow 4Al + 3O_2$$

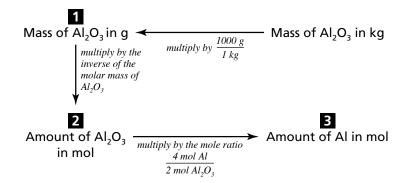
SOLUTION

- 1. ANALYZE
 - What is given in the the mass of aluminum oxide problem?
 - What are you asked to find? the amount of aluminum produced

Items	Data	
Substance	Al ₂ O ₃	Al
Coefficient in balanced equation	2	4
Molar mass	101.96 g/mol	NA
Amount	? mol	? mol
Mass	30.0 kg	NA

- 2. PLAN
 - What steps are needed to calculate the amount of Al produced from 30.0 kg of Al_2O_3 ?

The molar mass of Al_2O_3 can be used to convert to moles Al₂O₃. The mole ratio of Al: Al₂O₃ from the coefficients in the equation will convert to moles Al from moles Al₂O₃.



 $kg \stackrel{given}{Al_2} O_3 \times \frac{1000 \text{ g}}{kg} \times \frac{\frac{1}{\text{molar mass Al}_2 O_3}}{101.96 \text{ g Al}_2 O_3} \times \frac{\frac{mole \ ratio}{4 \text{ mol Al}}}{2 \text{ mol Al}_2 O_2} = mol \text{ Al}$

3. COMPUTE

 $30.0 \text{ kg Al}_2O_3 \times \frac{1000 \text{ g}}{\text{kg}} \times \frac{1 \text{ mol Al}_2O_3}{101.96 \text{ gAl}_2O_3}$ $\times \frac{4 \text{ mol Al}}{2 \text{ mol Al}_2 O_3} = 588 \text{ mol Al}$

4. EVALUATE

• Are the units correct? Yes; units canceled to give moles of

• Is the number of significant Yes; three significant figures is figures correct? correct.

• *Is the answer reasonable?* Yes; the molar mass of Al₂O₃ is about 100, so 30 kg of Al₂O₃ is about 300 mol. The mole ratio of Al: Al₂O₃ is 2:1, so the answer should be about 600 mol Al.

PRACTICE

1. Sodium carbonate reacts with nitric acid according to the following equation.

$$Na_2CO_3(s) + 2HNO_3 \rightarrow 2NaNO_3 + CO_2 + H_2O$$

a. How many moles of Na₂CO₃ are required to produce 100.0 g of NaNO₃? ans: 0.5882 mol Na₂CO₃

b. If 7.50 g of Na₂CO₃ reacts, how many moles of CO_2 are produced? ans: 0.0708 mol CO₂

2. Hydrogen is generated by passing hot steam over iron, which oxidizes to form Fe_3O_4 , in the following equation.

$$3\text{Fe}(s) + 4\text{H}_2\text{O}(g) \rightarrow 4\text{H}_2(g) + \text{Fe}_3\text{O}_4(s)$$

a. If 625 g of Fe₃O₄ is produced in the reaction, how many moles of hydrogen are produced at the same time? ans: 10.8 mol H₂

b. How many moles of iron would be needed to generate 27 g of hydrogen? ans: 10. mol Fe

SAMPLE PROBLEM 4

Methane burns in air by the following reaction:

$$CH_4(g) + 2O_2(g) \rightarrow CO_2(g) + 2H_2O(g)$$

What mass of water is produced by burning 500. g of methane?

SOLUTION

- 1. ANALYZE
 - What is given in the problem?

the mass of methane in grams

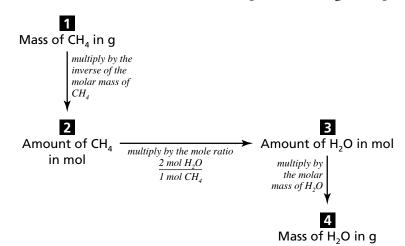
• What are you asked to find? the mass of water produced

Items	Data	
Substance	CH ₄	H ₂ O
Coefficient in balanced equation	1	2
Molar mass	16.05 g/mol	18.02 g/mol
Amount	? mol	? mol
Mass	500. g	? g

2. PLAN

• What steps are needed to calculate the mass of H_2O produced from the burning of 500. g of CH₄?

Convert grams of CH₄ to moles CH₄ by using the molar mass of CH₄. Use the mole ratio from the balanced equation to determine moles H₂O from moles CH₄. Use the molar mass of H₂O to calculate grams H₂O.



 $\begin{array}{l} \text{given} \\ \text{g CH}_{4} \times \frac{\frac{1}{\text{molar mass } \text{CH}_{4}}}{16.05 \text{ g CH}_{4}} \times \frac{2 \frac{\text{mole ratio}}{1 \text{ mol CH}_{4}}}{1 \text{ mol CH}_{4}} \times \frac{18.02 \text{ g H}_{2}\text{O}}{1 \text{ mol H}_{2}\text{O}} = \text{g H}_{2}\text{O} \end{array}$

3. COMPUTE

$$500. \text{ g-CH}_{4} \times \frac{1 \text{ mol-CH}_{4}}{16.05 \text{ g-CH}_{4}} \times \frac{2 \text{ mol-H}_{2}O}{1 \text{ mol-CH}_{4}} \times \frac{2 \text{ mol-H}_{2}O}{1 \text{ mol-H}_{5}O} = 1.12 \times 10^{3} \text{ g H}_{2}O$$

- 4. EVALUATE
 - Are the units correct? Yes; mass of H₂O was required, and units canceled to give grams H₂O.
 - Is the number of significant Yes; three significant figures is corfigures correct? rect because the mass of CH4 was given to three significant figures.
 - Yes; CH₄ and H₂O have similar mo-• *Is the answer reasonable?* lar masses, and twice as many moles of H₂O are produced as moles CH₄ burned. So, you would expect to get a little more than 1000 g of H₂O.

PRACTICE

1. Calculate the mass of silver bromide produced from 22.5 g of silver nitrate in the following reaction:

$$2AgNO_3(aq) + MgBr_2(aq) \rightarrow 2AgBr(s) + Mg(NO_3)_2(aq)$$

 $ans: 24.9 g AgBr$

2. What mass of acetylene, C_2H_2 , will be produced from the reaction of 90. g of calcium carbide, CaC₂, with water in the following reaction?

$$CaC_2(s) + 2H_2O(l) \rightarrow C_2H_2(g) + Ca(OH)_2(s)$$

ans: 37 g C_2H_2

3. Chlorine gas can be produced in the laboratory by adding concentrated hydrochloric acid to manganese(IV) oxide in the following reaction:

$$\mathsf{MnO}_2(s) \, + \, \mathsf{4HCl}(\mathit{aq}) \longrightarrow \mathsf{MnCl}_2(\mathit{aq}) \, + \, \mathsf{2H}_2\mathsf{O}(\mathit{l}) \, + \, \mathsf{Cl}_2(\mathit{g})$$

- a. Calculate the mass of MnO₂ needed to produce 25.0 g of Cl₂. ans: 30.7 g MnO₂
- **b.** What mass of MnCl₂ is produced when 0.091 g of Cl_2 is generated? ans: 0.16 g MnCl₂

ADDITIONAL PROBLEMS

1. How many moles of ammonium sulfate can be made from the reaction of 30.0 mol of NH₃ with H₂SO₄ according to the following equation:

$$2NH_3 + H_2SO_4 \rightarrow (NH_4)_2 SO_4$$

2. In a very violent reaction called a thermite reaction, aluminum metal reacts with iron(III) oxide to form iron metal and aluminum oxide according to the following equation:

$$Fe_2O_3 + 2Al \rightarrow 2Fe + Al_2O_3$$

- **a.** What mass of Al will react with 150 g of Fe₂O₃?
- **b.** If 0.905 mol Al₂O₃ is produced in the reaction, what mass of Fe is produced?
- c. How many moles of Fe₂O₃ will react with 99.0 g of Al?
- **3.** As you saw in Sample Problem 1, the reaction $N_2(g) + 3H_2(g) \rightarrow$ 2NH₃(g) is used to produce ammonia commercially. If 1.40 g of N₂ are used in the reaction, how many grams of H₂ will be needed?
- **4.** What mass of sulfuric acid, H₂SO₄, is required to react with 1.27 g of potassium hydroxide, KOH? The products of this reaction are potassium sulfate and water.
- 5. Ammonium hydrogen phosphate, (NH₄)₂HPO₄, a common fertilizer; is made from reacting phosphoric acid, H₃PO₄, with ammonia.
 - **a.** Write the equation for this reaction.
 - **b.** If 10.00 g of ammonia react, how many moles of fertilizer will be produced?
 - c. What mass of ammonia will react with 2800 kg of H₃PO₄?
- **6.** The following reaction shows the synthesis of zinc citrate, a ingredient in toothpaste, from zinc carbonate and citric acid.

$$3\text{ZnCO}_3(s) + 2\text{C}_6\text{H}_8\text{O}_7(aq) \rightarrow \text{Zn}_3(\text{C}_6\text{H}_5\text{O}_7)_2(aq) + 3\text{H}_2\text{O}(l) + 3\text{CO}_2(g)$$

- a. How many moles of ZnCO₃ and C₆H₈O₇ are required to produce $30.0 \text{ mol of } Zn_3(C_6H_5O_7)_2$?
- **b.** What quantities, in kilograms, of H₂O and CO₂ are produced by the reaction of 500. mol of citric acid?
- 7. Methyl butanoate, an oily substance with a strong fruity fragrance can be made by reacting butanoic acid with methanol according to the following equation:

$$C_3H_7COOH + CH_3OH \rightarrow C_3H_7COOCH_3 + H_2O$$

a. What mass of methyl butanoate is produced from the reaction of 52.5 g of butanoic acid?

- **b.** In order to purify methyl butanoate, water must be removed. What mass of water is produced from the reaction of 5800. g of methanol?
- **8.** Ammonium nitrate decomposes to yield nitrogen gas, water, and oxygen gas in the following reaction:

$$2NH_4NO_3 \rightarrow 2N_2 + O_2 + 4H_2O$$

- a. How many moles of nitrogen gas are produced when 36.0 g of NH₄NO₃ reacts?
- **b.** If 7.35 mol of H₂O are produced in this reaction, what mass of NH₄NO₃ reacted?
- **9.** Lead(II) nitrate reacts with potassium iodide to produce lead(II) iodide and potassium nitrate. If 1.23 mg of lead nitrate are consumed, what is the mass of the potassium nitrate produced?
- **10.** A car battery produces electrical energy with the following chemical reaction:

$$Pb(s) + PbO_2(s) + 2H_2SO_4(aq) \rightarrow 2PbSO_4(s) + 2H_2O(l)$$

If the battery loses 0.34 kg of lead in this reaction, how many moles of lead(II) sulfate are produced?

- 11. In a space shuttle, the CO_2 that the crew exhales is removed from the air by a reaction within canisters of lithium hydroxide. On average, each astronaut exhales about 20.0 mol of CO2 daily. What mass of water will be produced when this amount reacts with LiOH? The other product of the reaction is Li₂CO₃.
- **12.** Water is sometimes removed from the products of a reaction by placing them in a closed container with excess P₄O₁₀. Water is absorbed by the following reaction:

$$P_4O_{10} + 6H_2O \rightarrow 4H_3PO_4$$

- **a.** What mass of water can be absorbed by 1.00×10^2 g of P_4O_{10} ?
- **b.** If the P_4O_{10} in the container absorbs 0.614 mol of water, what mass of H₃PO₄ is produced?
- c. If the mass of the container of P₄O₁₀ increases from 56.64 g to 63.70 g, how many moles of water are absorbed?
- **13.** Ethanol, C₂H₅OH, is considered a clean fuel because it burns in oxygen to produce carbon dioxide and water with few trace pollutants. If 95.0 g of H₂O are produced during the combustion of ethanol, how many grams of ethanol were present at the beginning of the reaction?

14. Sulfur dioxide is one of the major contributors to acid rain. Sulfur dioxide can react with oxygen and water in the atmosphere to form sulfuric acid, as shown in the following equation:

$$2H_2O(l) + O_2(g) + 2SO_2(g) \rightarrow 2H_2SO_4(aq)$$

If 50.0 g of sulfur dioxide from pollutants reacts with water and oxygen found in the air, how many grams of sulfuric acid can be produced? How many grams of oxygen are used in the process?

- **15.** When heated, sodium bicarbonate, NaHCO₃, decomposes into sodium carbonate, Na₂CO₃, water, and carbon dioxide. If 5.00 g of NaHCO₃ decomposes, what is the mass of the carbon dioxide produced?
- **16.** A reaction between hydrazine, N_2H_4 , and dinitrogen tetroxide, N2O4, has been used to launch rockets into space. The reaction produces nitrogen gas and water vapor.
 - **a.** Write a balanced chemical equation for this reaction.
 - **b.** What is the mole ratio of N_2O_4 to N_2 ?
 - c. How many moles of N₂ will be produced if 20 000 mol of N₂H₄ are used by a rocket?
 - **d.** How many grams of H_2O are made when 450. kg of N_2O_4 are consumed?
- 17. Joseph Priestley is credited with the discovery of oxygen. He produced O₂ by heating mercury(II) oxide, HgO, to decompose it into its elements. How many moles of oxygen could Priestley have produced if he had decomposed 517.84 g of mercury oxide?
- **18.** Iron(III) chloride, FeCl₃, can be made by the reaction of iron with chlorine gas. How much iron, in grams, will be needed to completely react with 58.0 g of Cl₂?
- 19. Sodium sulfide and cadmium nitrate undergo a double-replacement reaction as shown by the following equation:

$$Na_2S + Cd(NO_3)_2 \rightarrow 2NaNO_3 + CdS$$

What is the mass, in milligrams, of cadmium sulfide that can be made from 5.00 mg of sodium sulfide?

20. Potassium permanganate and glycerin react explosively according to the following equation:

$$14KMnO_4 + 4C_3H_5(OH)_3 \rightarrow$$

$$7K_2CO_3 + 7Mn_2O_3 + 5CO_2 + 16H_2O$$

- a. How many moles of carbon dioxide can be produced from 4.44 mol of KMnO₄?
- **b.** If 5.21 g of H₂O are produced, how many moles of glycerin, $C_3H_5(OH)_3$, were used?

- c. If 3.39 mol of potassium carbonate are made, how many grams of manganese(III) oxide are also made?
- **d.** How many grams of glycerin will be needed to react with 50.0 g of KMnO₄? How many grams of CO₂ will be produced in the same reaction?
- 21. Calcium carbonate found in limestone and marble reacts with hydrochloric acid to form calcium chloride, carbon dioxide, and water according to the following equation:

$$CaCO_3(s) + 2HCl(aq) \rightarrow CaCl_2(aq) + CO_2(g) + H_2O(l)$$

- **a.** What mass of HCl will be needed to produce 5.00×10^3 kg of
- **b.** What mass of CO₂ could be produced from the reaction of 750 g of CaCO₃?
- 22. The fuel used to power the booster rockets on the space shuttle is a mixture of aluminum metal and ammonium perchlorate. The following balanced equation represents the reaction of these two ingredients: $3Al(s) + 3NH_4ClO_4(s) \rightarrow$

$$Al_2O_3(s) + AlCl_3(g) + 3NO(g) + 6H_2O(g)$$

- a. If 1.50×10^5 g of Al react, what mass of NH₄ClO₄, in grams, is
- **b.** If aluminum reacts with 620 kg of NH₄ClO₄, what mass of nitrogen monoxide is produced?
- 23. Phosphoric acid is typically produced by the action of sulfuric acid on rock that has a high content of calcium phosphate according to the following equation:

$$3H_2SO_4 + Ca_3(PO_4)_2 + 6H_2O \rightarrow 3[CaSO_4 \cdot 2H_2O] + 2H_3PO_4$$

- a. If 2.50×10^5 kg of H₂SO₄ react, how many moles of H₃PO₄ can be made?
- **b.** What mass of calcium sulfate dihydrate is produced by the reaction of 400. kg of calcium phosphate?
- **c.** If the rock being used contains 78.8% Ca₃(PO₄)₂, how many metric tons of H₃PO₄ can be produced from 68 metric tons of rock?
- 24. Rusting of iron occurs in the presence of moisture according to the following equation:

$$4\text{Fe}(s) + 3\text{O}_2(g) \rightarrow 2\text{Fe}_2\text{O}_3(s)$$

Suppose that 3.19% of a heap of steel scrap with a mass of 1650 kg rusts in a year. What mass will the heap have after one year of rusting?